# DIGITAL LOGIC HANDBOOK



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# INTRODUCTION

DEC Digital Modules are a coordinated set of digital circuits used for building and testing computer systems.

For use as laboratory equipment, they are packaged for convenient patch cord interconnections. For use in systems, they are packaged in a unique plug-in unit construction. They are available in three compatible speed ranges with maximum frequencies of 500 kilocycles, 5 megacycles, and 10 megacycles.

DEC Modules are designed to be easy to understand and easy to use. People with no knowledge of Boolean algebra can perform logical design with DEC Modules, and those who like to use Boolean mathematics can very quickly and easily implement their equations. Straightforward static logic is employed, and only a small number of Modules is needed for most systems because of the high driving capability of each unit.

The general logical principles utilized are the same for all Modules. The purpose of this booklet is to acquaint the reader with these principles.

The logic used with DEC Modules is "static." "ONES" and "ZEROS" in this system are represented by two different DC voltage levels. The use of such a static system makes it possible to change the state of a system at any time. Logic is performed by the coincidence of levels which are sampled by pulses. Unlike "dynamic" logic, where ONES and ZEROS are represented by the presence or absence of a train of pulses, static logic is not tied to a fixed clock frequency and usually avoids precise timing problems.

The rules governing loading will depend on the speed range of the equipment used. The rules and illustrations in this book are applicable principally to 500 kilocycle and 5 megacycle Modules.



DEC LABORATORY MODULES (TOP) AND DEC SYSTEM MODULES ARE AVAILABLE IN THREE COMPATIBLE FREQUENCY RANGES

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DEC SYMBOLOGY		
A small rectangle with an enclosed solid triangle is an inverter.	Base Input Emitter INVERTER	
A resistor with a large solid dot is a standard DEC clamped load resis- tor.	CLAMPED LOAD	
The solid diamond is a logic level for which the assertion level is —3 volts.	LEVEL – NEGATIVE	
The open diamond is a logic level for which the assertion level is ground.	LEVEL - GROUND	
The solid arrowhead is a negative pulse (from ground).	PULSE – NEGATIVE	
The open arrowhead is a positive pulse (from ground).	→ PULSE – POSITIVE	
Arrowheads (or diamonds) are used at all branch points to indicate signal flow.		

# **BASIC DIGITAL MODULES**

# THE TRANSISTOR INVERTER

Most logical operations with DEC Modules are performed with saturating PNP transistor inverters. When a junction transistor is turned completely on or "saturated," the collector is practically a short circuit to the emitter of the transistor. If the emitter is at ground in this condition, the output from the collector will also be at ground voltage.

When a junction transistor is turned completely off or "opened," the collector-to-emitter path is practically an open circuit. If the collector is connected to a clamped load resistor, the collector will be at -3 volts.



Figure 1 is a schematic drawing of a DEC inverter and clamped load resistor. The capacitor shunting the input resistor is used to provide overdriving current to the transistor during input level changes, thus switching the transistor much more rapidly. The resistor to  $\pm 10$  volts biases off the transistor to protect against noise voltage. The load resistor is clamped to -3 volts with a diode so that, when the transistor is off, the output signal is always at -3volts regardless of the loading on the inverter output. To simplify logic drawings, the symbology of Figure 2 is used. When the input is negative, the output is "shorted" to ground. When the input is positive or at ground level, the transistor is open circuited and the output, if connected to a clamped load resistor, is at -3 volts.



FIGURE 3

The inverter switch is analogous to the mechanical switch, as shown in Figure 3. The logical designer can often build networks of inverters in the same manner as he would if he were using mechanical relays or simple switches.



Figure 4 shows three mechanical switches connected in a series to form an "AND" circuit. All switches A and B and C must be closed in order to ground the output. Similarly, in the series inverter network of Figure 5, all transistor inputs A and B and C must be negative in order to short the output to ground. If any input in Figure 5 is ground, that transistor will be an open circuit, and the output will be -3 volts. Therefore, the network also acts as an "OR" circuit for ground levels.

If any of the switches of Figure 6 close, the output will be shorted to ground. If A or B or C in Figure 7 is negative, the output will be shorted to ground. Only if all inputs are at ground will the network output be negative. The parallel arrangement in Figure 7 is an OR gate for negative levels and an AND gate for ground levels.



Inverters can be stacked in complicated series-parallel combinations, like that of Figure 8, to perform sophisticated logical operations. There are some rules, however, since the inverters are not quite ideal switches. These rules are discussed in the sections beginning on Page 41.



# DIODE LOGIC

All logical systems could be constructed using only parallel and series combinations of transistors in inverter networks. However, as the number of inputs to a particular gate increases, it becomes more economical to perform the gating action with diode gates. The



INTERIOR VIEW OF 5 MEGACYCLE LABORATORY MODULE



LABORATORY MODULE MOUNTING PANEL SHOWING POWER CONNECTIONS AT THE BACK

outputs of diode gates are permanently connected to a transistor inverter which re-establishes the reference level after every gate. Thus, DEC diode gates may be connected in tandem indefinitely.



FIGURE 9

DEC negative diode units are six-input diodes tied to an inverter, as in Figure 9, so that any one of the input terminals can turn on the inverter. This makes a six-input OR circuit for negative levels or pulses because A, B, C, D, E, or F can turn on the inverter and "short circuit" its output. This, of course, also acts as an AND circuit for ground levels.



The positive-type diode circuit, Figure 10, provides an AND circuit for negative levels and an OR circuit for ground levels. This unit is available only in DEC System Modules because DEC Laboratory Modules are usually employed in small systems and the economy resulting from the use of this type of unit is small.

## **FLIP-FLOPS**

If two grounded inverters are interconnected, as in Figure 11, a bi-stable "flip-flop" is obtained. When one side is cut off, its output is negative. This holds the other side on, which, in turn, holds the first side off.



FIGURE 11

If a grounded inverter A is connected to the off side B of the flipflop in Figure 12, the state of the flip-flop can be changed by pulsing the base of transistor A with a negative signal. This extra transistor will short the collector of transistor B to ground and will cut off transistor C, which will turn on transistor B. The flip-flop will then stay in that state even after the signal is removed from A.



FIGURE 12

Simple flip-flops, such as in Figure 12, can be used wherever the load on the output is light and economy is important. DEC System Modules Types 1213 and 4213 contain circuits similar to this one.

For general applications, it is desirable to have flip-flops with very low output impedance so that they can drive many other circuits. For this reason, most DEC flip-flops have buffer amplifiers on each side of the flip-flop.



A simple network is placed between the flip-flop in Figure 13 and the output amplifiers, which delays the change in the output. When the flip-flop is changed with a standard pulse, this delay is long enough so that the output does not change until after the pulse is over. This allows flip-flops to be sensed while they are being pulsed, which makes shift registers, counters and adders relatively simple.



FIGURE 14

The symbol for a flip-flop is shown in Figure 14. In order to set the flip-flop to the desired state, the inputs at the bottom are "shorted" through inverters to ground. When the input on the ZERO side has been shorted to ground, the ZERO output is set to the -3 volt level and the ONE output is at ground. This is defined as the ZERO state. Similarly, when the flip-flop is in the ONE state, the ONE output is at -3 volts and the ZERO output is at ground.



FIGURE 15

FIGURE 16

Flip-flops are always changed by momentarily shorting an input to ground, as shown in Figure 15. The input to the inverter is a DEC Standard Negative Pulse of 2.5 volts amplitude relative to ground.

To gate information into a flip-flop, two inverters can be connected in series, as in Figure 16. If the level input is at ground when the upper inverter is pulsed, the flip-flop terminal will not be shorted to ground; but if the level input is at -3 when the negative pulse arrives, the input is shorted and the flip-flop is cleared.

Since most DEC flip-flops have buffer amplifiers, it is permissible to use the buffer as the level gate. This added flexibility is useful since it allows reading into a flip-flop with only one inverter gate.



FIGURE 17

Figure 17 is a "jam transfer" gate employing DEC buffered flipflops. The contents of flip-flop A can be "jammed" into flip-flop B with a single pulse independent of the previous state of flip-flop B. The outputs of A are connected directly to the emitters of the pulse gates feeding the inputs of B. Both inverter pulse gates are pulsed simultaneously, but only the gate which has ground on its emitter will pass the pulse to set the flip-flop. For example, if flip-flop A holds a ONE, its ZERO output terminal will be at ground, allowing the right-hand gate to pass the pulse and set flip-flop B.



The shift register of Figure 18 is another use of the jam transfer gate of Figure 17. Since the outputs of the flip-flops do not change until the shift pulse has passed, no logical delays are needed between flip-flops.



10 MEGACYCLE SYSTEM MODULE FLIP-FLOP



System Module Mounting Panel with Unit Extender

When the inverters of Figure 19 are pulsed, the state of the flipflop will be changed or "complemented." On some of the DEC flip-flops this gating is done internally, and a complement terminal is brought out, as in Figure 20.



There is also a complement output terminal P which will deliver a DEC Standard Negative Pulse every time the flip-flop complement input is pulsed. This P pulse output is useful in counters and adders.



FIGURE 21

A typical counter arrangement using DEC complementing flipflops is shown in Figure 21. The pulses being counted enter on the right. They always complement flip-flop C and generate a standard pulse at P. This P pulse complements flip-flop B when flip-flop C holds a ONE. When this P pulse gets through the gate and actually complements B, it will generate a P pulse out of B. The process is continued down the length of the counter. Only one inverter and one flip-flop are needed for each bit in the counter.



System Module flip-flops also have direct clear and set terminals which allow flip-flop registers to be set or cleared without the use of pulse gates on each flip-flop. The input to these terminals is a DEC Standard Positive Pulse of 2.5 volts amplitude relative to ground. These pulses can be produced by DEC delays, pulse amplifiers, clocks, and pulse generators. Figure 22 shows a register being set to 00100 using the direct inputs.

## DELAYS

DEC Delay units are flip-flops which have only one stable state. When the input terminal is "shorted" to ground by a Standard Pulse, the level output terminal will switch from its normal ground level to the -3 volt level for a fixed period of time, which is adjustable. A standard pulse will be produced at the pulse output when the level output returns to its normal 0 volt condition. The pulse output comes from a pulse transformer which has both terminals available. To obtain a negative pulse, ground the output from the positive terminal. To obtain a positive pulse, ground the output from the negative terminal.



FIGURE 23

Typical waveforms for a delay unit are shown in Figure 23.



FIGURE 24

Delay units are particularly useful in generating delayed standard pulses or signals of arbitrary width. The network of delays in Figure 24 will produce the waveform in Figure 25.



FIGURE 25

# PULSE AMPLIFIERS

DEC pulse amplifiers are a powerful logical element because they not only amplify and standardize the shape of pulses but also gate pulses. When the same logical gating is to be done on a whole register of flip-flops, it often can be done once before the pulse amplifier drives the register.



FIGURE 26

The outputs of the pulse amplifiers come from pulse transformers, which have both terminals available so that either positive or negative pulses may be obtained, depending on which terminal is grounded. Positive pulses are used to direct set and clear flip-flops without inverters. Negative pulses are used for setting, clearing and complementing with inverters.

# CLOCKS

DEC clocks produce standard pulses from stable, variable frequency, RC-coupled oscillators which have a wide range of frequencies available. These clocks are often used as a primary source of timing for large systems. Where very precise timing is needed, crystal clocks which contain a single-frequency crystal oscillator are available.



FIGURE 27

# PULSE GENERATORS

DEC pulse generators are used to initiate action as a result of outside activity. Every time the input of these pulse generators goes more negative than  $-2\frac{1}{2}$  volts after having been more positive than -1 volt, a standard pulse is generated. Most outside actions can be converted into voltage levels that will fill this criterion.



FIGURE 28

It is difficult to generate a single pulse from a switch or relay closure because contacts bounce many times before they finally make a solid contact. If these are connected directly to a pulse generator, they will produce a pulse for each contact bounce. An integrating circuit is included which can be connected between the pulse generator and the contact. This circuit converts the many fast voltage changes into a single slow change, which generates a single pulse.



FRONT VIEW OF DEC SYSTEM MODULE MOUNTING PANEL SHOWING STANDARD PIN CONNECTIONS



FRONT VIEW OF NEW TAPER-PIN MOUNTING PANEL WHICH PERMITS PATCHCORDING OF SYSTEM MODULES

# TYPICAL APPLICATIONS

#### COUNTERS

Building a counter with DEC flip-flops is straightforward due to the built-in delay and the availability of the P pulse terminal. A carry pulse is created when the P pulse is fed to the base of a gate which is conditioned by the ONE state of the flip-flop.

## STRAIGHT BINARY COUNTING



(DEC Flip-Flops Type 201, 1201, 3201, or 4201)

When flip-flop D in Figure 29 is in the ONE state, its ZERO output terminal is ground. When it receives a complement pulse, the gate will pass a P pulse into the complement input terminal of flip-flop C. If flip-flop D had been in a ZERO state, the P pulse would have been prevented from complementing flip-flop C. The series connection of P pulses and gates is the high-speed carry chain. The carry propagate time per digit is much less than the flip-flop's total transition time.

To assure that flip-flop D will not be in the process of changing state while flip-flop C is receiving its carry pulse, a delay has been built into each flip-flop package. This insures that the ONE and ZERO output terminals will not change until after the carry pulse has been gated.

Each bit of the counter requires one flip-flop and one transistor gate. There are two gates contained in each DEC Flip-Flop Type 201, 1201, 3201, and 4201. If DEC Laboratory Modules are used, the results can be read by means of the indicator lights on the front panel. DEC System Modules Types 1201 and 4201 are compatible with Indicator Drivers Types 1675 and 1669, which are suitable for driving remote indicator lights.

## Special Counts

Often it is desirable to build a counter that will produce a signal after a particular number (N) of events have occurred. If N is an integer power of 2, the output is automatically produced by the final digit of a counter of appropriate length. If N is not a power of 2, gating must be performed to detect the desired number, generate a signal, and reset the counter to 0.



FIGURE 30 ARBITRARY COUNT — COUNT OF 12 ILLUSTRATED (DEC Flip-Flops Type 201, 1201, 3201, or 4201)

Transistor inverter gates or diode gates may be used to sense the number N-1, close the input to the counter, and re-route the Nth input pulse so that it will clear the counter and generate an output signal. Although this is not always the optimum method, it is a completely general method which will work for any value of N.



FIGURE 31 COUNT OF 3 (DEC Flip-Flops Type 201, 1201, 3201, or 4201)

A typical counting sequence is shown for N = 3 in Figure 31. The progress of the count is shown in the table. When the count of 2 is reached, the next pulse will clear the counter and generate an output signal.



FIGURE 32 COUNT OF 6 (DEC Flip-Flops Type 201, 1201, 3201, or 4201)

A counter for 6 is made from the counter for 3 by preceding it with a binary counter (Figure 32). Examination of the counting sequence shows that the least significant digit alternates between ZERO and ONE, while the two most significant digits follow the same pattern as the count of 3. The circuit for flip-flops A and B is identical to that for the count of 3 except that two additional gates are necessary. These are required because the input to the count-of-3 portion includes a conditioning level, as well as a pulse.

0 Ô COUNTING OFFA <sup>0</sup> FF C<sup>1</sup> FFB SEQUENCE 000 0 001 1  $\overline{2}$ 010 3 011 Pulses 4 100 To Be Counted

BINARY CODED DECIMAL COUNTING

FIGURE 33 COUNT OF 5 (DEC Flip-Flops Type 201, 1201, 3201, or 4201)

From the simple count-of-5 circuit, binary coded decimal counters may be generated.



FIGURE 34 COUNT OF 10 — BINARY CODED DECIMAL (DEC Flip-Flops Type 201, 1201, 3201, or 4201)

To give a count of 10, the counter for 5 is preceded by a binary counter (Figure 34). This circuit is compatible with DEC's BCD Decoder and Light Driver Type 1671, which has 10 output lines for driving a decimal output display.

A counter for 100 can be made by cascading two BCD stages. Because the complement input to A is used only at the time the decade is cleared, the P pulse can feed the next stage without being gated. Any number of BCD stages may be cascaded in a similar manner.



UP COUNTERS AND DOWN COUNTERS ARE AMONG THE LOGICAL OPERATIONS WHICH CAN BE PERFORMED WITH THE DEC BASIC LOGIC KIT



FIGURE 35 DOWN COUNTER (DEC Flip-Flops Type 201, 1201, 3201, or 4201)

In a down counter, each successive pulse will decrease the count by 1. The method for building a down counter is essentially the same as that used in the up counter, except that each flip-flop input is conditioned by the ZERO state of the previous flip-flop. In this way, the P pulse chain will form a high-speed borrow circuit instead of a carry circuit.



FIGURE 36 BINARY UP-DOWN COUNTER (DEC Flip-Flops Type 1201 or 4201)

An up-down counter combines the techniques found in the individual up and down counters. This is made possible by use of DEC Flip-Flops Type 1201 or 4201. Each of these units contains a flip-flop with two independent sets of complement and associated P pulse terminals. Thus, it is possible to connect one set to form a high-speed carry circuit, while the other set forms a high-speed borrow circuit. Of course, the add and subtract pulses should not be allowed to arrive simultaneously.

10 Megacycle Counting



10 MC BINARY COUNTER (DEC Flip-Flops Type 5201 or 6201)

The logic behind a 10 megacycle counter is the same as that for a 5 megacycle or 500 kilocycle counter; however, the loading rules differ. Two inverters are required for each bit. The pulse must go to the lower inverter, as shown, to insure sufficient pulse gain to propagate the carries.

Only one 10 megacycle flip-flop is needed for counting at 10 megacycles where carry propagate time is not important. Such a mixed system is shown in Figure 38. In the transition from one type of equipment to another, a pulse amplifier with feedback is required to lengthen the pulse.

# PARALLEL ADDERS

Addition of the contents of the incident number register to the contents of the accumulator is accomplished in two discrete steps, a half-add and a carry. This is made possible by using DEC Flip-Flops Types 1201 or 4201 as in Figure 39. These units have two discrete complement inputs, each with its own P pulse terminal.

The first step is half-add. Each digit of the accumulator is complemented if the corresponding digit of the incident number is a ONE.



FIGURE 38 10 MC COUNTER, MIXED SYSTEM — SHOWING PULSE STRETCHING (Lower cost than Figure 37 counter, but longer propagate time)



FIGURE 39 PARALLEL ADDER (Accumulator Flip-Flops DEC Type 1201 or 4201)

The second step is carry. A carry will be generated if a digit in the accumulator is ZERO and the corresponding incident number digit is ONE. A carry will be propagated if an accumulator digit is ONE and it also receives a carry pulse from the next less significant accumulator digit. After the carries have propagated, the contents of the incident number register may be modified to add another number to the accumulator.

Table I provides some examples.

Incident Number	Original Accumulator Number	Accumulator After Half-Add	Accumulator After Carry
001	010	011	011
001	001	000	010
001	011	010	100

TARFET	TABLE	: ]
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MEMORY CORE EVALUATOR MADE FROM DEC LABORATORY MODULES

Variations of this technique can be used to make a subtracter, a multiplier, a divider, etc. A faster adder can be built by using 10 megacycle Flip-Flops Type 6202, as shown in Figure 40.



FIGURE 40 PARALLEL ADDER USING 10 MC FLIP-FLOPS (Accumulator Flip-Flops DEC Type 6202)

## COMPARATORS

# Comparing a Toggle Switch Register and a Flip-Flop Register

The simplest comparator is the type used in building a counter which will stop or reset itself after a preset number of counts. This type of comparator, as illustrated in Figure 30, consists merely of a string of diode gates with each diode connected through a toggle switch to a flip-flop. Each toggle switch corresponds to a single binary bit, with a closed switch representing a ONE and an open switch representing a ZERO. Since opening a toggle switch has the same effect as removing the corresponding diode, there may be several numbers which would generate a comparator output. However, the first comparator output will correspond to the desired number if the counter always begins in the all ZERO state. This, of course, requires that the counter be reset, or the counter input be terminated as soon as the comparator output appears.

The comparator output, in Figure 30, is used to close the counter input and re-route the next count pulse to perform the clearing action. Since this action requires an additional input pulse, the toggle switches must be set to detect one less than the desired number. This technique can also be used with a down counter. The diode gates are then connected to the flip-flops so that a closed switch corresponds to a ZERO. The first comparator output is used to preset the counter to the all ONE state or to turn off the counter input.

Comparing a toggle switch register with an arbitrary flip-flop register requires a single-pole double-throw switch for each bit. Thus both ZEROS and ONES are detected.

#### COMPARING TWO FLIP-FLOP REGISTERS

Comparison of two flip-flop registers requires an "EXCLUSIVE OR" for each corresponding pair of bits, since there are two possible conditions which will produce an inequality; i.e., bit A1 = 0 and B1 = 1 or A1 = 1 and B1 = 0. The entire set of EXCLUSIVE OR'S must then be OR'd together to determine when any pair of bits is unequal.

Figure 41 shows an example of a two-register comparator. The EXCLUSIVE OR'S consist of two inverters. The final ORing function is accomplished by simply tying the inverter outputs together. Whenever the two bits of any pair are different, the comparator output will be at ground. When there are no differences, the output will be negative.



(10 mc, 5 mc or 500 kc Inverters)

Of course, there is a limit to the number of inverters which can be connected in this manner. If a single standard clamped load resistor is used to define the —3 logic level, then the maximum number of "on" bases is six (as explained in the section entitled "Loading Definitions" and the technical literature describing the inverters). Since only one base in each EXCLUSIVE OR pair can be "on" at a time, the maximum configuration is actually seven pairs of inverters. To increase the allowable number of inverters, the clamped load resistor may be replaced by a 10,000 ohm resistor externally wired to the —15 volt terminal. The maximum configuration is then 14 pairs of inverters; however, the output can drive only one inverter base.



FIGURE 42 COMPARATOR (DEC Diodes Type 4113)

Figure 42 shows an equivalent comparator with the inverters replaced by two-input diode units. Here the load determining factor is the  $i_{co}$  of the transistors. If only one unit Base Load is to be supplied by the output, then up to 100 pairs of diode gates may be used. If the number of pairs of diode gates is decreased, then the output driving ability is increased proportionally.

#### SIGN OF AN INEQUALITY

A more sophisticated comparator is used to compare the numerical value of two registers to determine equality or the sign of an inequality. This problem requires that each pair of bits be investigated in the order of their significance. Once an inequality has been discovered, all further investigation must be stopped so that the differences in bits of lesser significance will not affect the output.

Figures 43 and 44 show the  $i^{th}$  stage of such a comparator chain. To begin investigation, the equality line is brought to -3 volts. This negative signal is ANDEd with an EXCLUSIVE OR for the first pair of bits. If there is equality, then the negative signal will propagate down the equality line. If all corresponding pairs of both registers are equal, the negative signal will appear at the end of the final stage. However, if an inequality is reached, further investigation will be stopped and the equality line output will remain at ground. If this inequality is such that register A is greater than register B, then a ground signal will be generated at the sign output.



FIGURE 43 COMPARATOR (DEC Diodes Type 1111 or 4111)



FIGURE 44 COMPARATOR (DEC Diodes Type 4113)

There is no limit to the number of stages through which the equality line may propagate. The restrictions on the sign output are similar to those described in the previous section. In Figure 43 the sign output is fed by diode units with grounded emitters. Thus, the output will drive one unit base load if it is fed by one clamped load resistor and up to 100 diode gates.

With the configuration for the sign output as shown in Figure 44, it may be necessary for a single "on" transistor to supply the base current for other transistors with both negative bases and emitters. If a standard clamped load resistor is used to define the output level, then a maximum of seven inputs may be connected. If the clamped load resistor is replaced by a 10,000 ohm resistor wired to the -15 volt terminal, then the maximum number of inputs is 14.

#### PARITY GENERATOR

A Parity Generator is a comparator which compares flip-flops within the same register. The circuits shown in Figures 45 and 46 are made up of EXCLUSIVE OR'S as in the previous examples. Each EXCLUSIVE OR determines whether the sum of its two inputs is odd or even. The circuits are built up in a pyramid arrangement so that the output of the final EXCLUSIVE OR gives the parity of the sum of all the inputs.



FIGURE 45 PARITY CIRCUIT (5 mc or 500 kc Inverters)

To lighten the load on the inverters, 10,000 ohm resistors are used instead of standard clamped load resistors. The maximum series configuration is three inverters or one inverter and one 2-input diode gate. When the emitter of an inverter is driven from a flip-flop output (Figure 45), the flip-flop must be counted as an inverter.



FIGURE 46 PARITY CIRCUIT (DEC Diodes Type 4113)

## SYNCHRONIZERS

Synchronizers are extremely important in any digital system, not only to determine what will happen if two asynchronous or incompatible signals occur, but also to assure that catastrophic errors will not result from such signals. Asynchronous signals are often commands such as start, stop or clear. Incompatible signals must be guarded against whenever a single flip-flop register is connected for more than one possible mode of operation.

Some typical cases where synchronizers are required are as follows:

1. Shift Registers — When a shift register is being changed from parallel mode to serial mode or vice versa, care must be taken that a split or partial pulse is not allowed to enter the system. Such a pulse could result in a partial shift, partial read-in or partial read-out. Likewise, a bi-directional shift register should never be commanded to shift left and shift right at the same time.

2. Counters — Particular care must be taken with start or stop signals which occur at random times relative to the counter input. If a synchronizer is not used, this situation might result in a split or partial pulse which would enter the system and propagate only part way down the carry chain. Thus, the entire number in the counter, or any part of that number, could be wiped out. A similar split pulse might occur in a bidirectional counter if the add and subtract inputs were pulsed simultaneously. Basically, a synchronizer is accomplished by ANDing together a random input signal and a primary pulse stream (usually a clock) and feeding the results of this AND gate into a single flip-flop. If the random signal arrives while the clock pulse is occurring, the single synchronizer flip-flop makes the decision as to whether the signal will be accepted or rejected. Provision must also be made for the rejected signal to be accepted by the next clock pulse; thus, the input signal may be slightly delayed by the synchronizer flip-flop, but there will be no "middle" state which would activate only a portion of the main circuit.

#### LEVEL SYNCHRONIZER

Figure 47 shows a method of synchronizing a command level, such as a mode control, with a primary pulse stream. When the input level is ground, the primary pulse stream will pass through terminal A. When the input level is negative, the primary pulse stream will pass through terminal B. If the input level is in the process of changing at the time the clock pulse occurs, then the decision to accept or reject the signal change will be made by the synchronizer flip-flop only. Thus, no pulses will ever pass out both terminal A and terminal B, and no split pulses will ever pass out either terminal. This method, or a variation, is often used in controlling the direction of count in an up-down counter.



FIGURE 47 LEVEL SYNCHRONIZER (DEC Flip-Flops Type 201, 1201, 1209, 3201, 4201, or 4209)

#### START-STOP SYNCHRONIZER

Figure 48 shows a method for synchronizing start and stop commands with a primary pulse stream. This type of synchronizer is extremely important in counters which are used to measure time intervals.



FIGURE 48 START STOP SYNCHRONIZER (DEC Flip-Flops Type 201, 1201, 1209, 3201, 4201, 4209, 5202, or 6202)

The random start and stop pulses will be converted to stop or start levels by flip-flop A. Flip-flop B will convert this randomly changing level into a level that changes synchronously with the primary stream. This level, in turn, conditions the output pulse stream. The action may be delayed by one clock pulse. However, a split pulse will never be allowed to enter the main system.

#### SINGLE PULSE SYNCHRONIZATION

Figure 49 shows a method for synchronizing a single pulse with a primary stream of pulses. The operation of the synchronizer is similar to that of Figure 48 except that the stop command is automatically generated by the first pulse to leave the synchronizer. Thus, one, and only one, pulse will pass into the main system, and this pulse will be synchronized with the main system.



FIGURE 49 ONE PULSE SYNCHRONIZER (DEC Flip-Flops Type 201, 1201, 1209, 3201, 4201, or 4209)

#### SUBTRACTERS

An adder may be used for subtraction as well as addition. To subtract a number from the accumulator, the number is made negative and added to the accumulator. The steps involved in performing a subtraction depend on whether the "one's complement" or the "two's complement" number system is used to represent a negative number.

The "one's complement" number system is easiest to implement. To subtract a number from the accumulator, the steps are: (1) complement the incident number, (2) half-add, and (3) carry. With this number system it is necessary to implement an "end-around carry" from the most to the least significant digit. This connection is shown in Figures 39 and 40.

Subtraction is performed in DEC's PDP computers by (1) complementing the accumulator, (2) half-add, (3) carry, and (4) recomplementing the accumulator.

# GRAY-TO-BINARY CODE CONVERTER

A frequent problem in digital control work is to convert a Gray coded number, such as a shaft position, into a pure binary number so that it can be used conveniently in arithmetic operations. The DEC converter begins examination with the most significant bit and proceeds down the line, making use of two basic conversion principles: (1) the most significant digit is identical in Gray and binary and (2) if a digit is a 1 after being converted to binary, the following digit is complemented. The DEC converter does not require any shifting or transferring of information. All logic is done by means of inverter gates, arranged in such a way that the convert pulse will simultaneously convert all digits from Gray to binary.



FIGURE 50 GRAY-TO-BINARY CONVERTER (DEC Flip-Flops Type 201, 1201, 3201, 4201, 4209, 5202, or 6202)

# **RULES AND DEFINITIONS**

# **INVERTER USAGE**

#### 5 mc and 500 kc Modules

DEC transistor inverters serve two functions. When used as level gates, they are placed in series and parallel configurations to perform logic. When used as pulse gates, the inverter will sample the logic performed by the level gates and read the results into a flip-flop or other active element.

When used as a pulse gate, an inverter will drive one and only one pulse unit. Inverters serving as level gates are usually considered as simple switches when designing logical networks, but because they are not ideal switches, there are certain limitations which have to be taken into account. The voltage drop across saturated inverters is not zero; it is closer to 0.1 volt. As a result, inverters cannot be stacked indefinitely. Three inverters is the maximum which can be put in series if the output is to drive another inverter, as in Figure 51.



If inverters are in series with the output of a flip-flop, as in Figure 52, the flip-flop buffer inverter is considered to be one of the three allowed series transistors.

When the output of a series of inverters is driving the input of a pulse amplifier or delay unit or the set or clear input of a flip-flop, as in Figure 53, a fourth transistor serving as a pulse gate may be added in series. Only three may be used in series when driving the complement input of a flip-flop.

It is important to note that a clamped load resistor is tied to the emitter of each pulse transistor when it is being driven from an inverter or a network of inverters, as in Figure 53.



FIGURE 53\*

Because inverters are not really ideal switches, each collector of a series string of DC inverters supplying a pulse inverter will go somewhat negative during the pulse. This means that, if a series of inverters is supplying both pulse current and a DC signal, care must be taken because a signal will occur in the DC output during the pulse.



In Figure 54, when the input C is negative, flip-flop A should be set by the pulse, but flip-flop B should not be set. However, during the pulse, collector E of the DC inverter feeding flip-flop A will go slightly negative. It will partly turn on the DC inverter feeding flip-flop B, and sometimes it will set flip-flop B as well as flip-flop A. This network will work only if the pulses are not simultaneous.

<sup>\*</sup>The clamped load resistor is not needed in 5 megacycle circuitry when the pulse inverter is driven from a single series of inverters and the length of wire between inverters is short.

In the 500 kilocycle line this clamped load resistor can be replaced by a 1N276 diode from the emitter of the pulse inverter to ground, connected so as to prevent this point from going positive.



Construction of Digital Systems, such as this DEC Memory Tester, Is Greatly Simplified by the Use of System Modules



MOUNTING PANELS MAY BE PRE-WIRED TO FORM SYSTEM SUB-ASSEMBLIES



FIGURE 55

The network shown in Figure 55 will work whether or not the pulses are simultaneous. Two additional inverters have been added so that collector E will no longer be pulled negative by the pulse, since the pulse current will now come directly from ground instead of collector E. (If both outputs are feeding the same flip-flop, the network shown in Figure 54 can be used safely because the output of the A side will be much greater than that of the B side.)

# LOADING DEFINITIONS

To facilitate the design of systems, a number of simple loading definitions and rules have been made. These do not cover all possible configurations, but they do serve as a useful guide.

A "BASE LOAD" is the current which must be taken from the base of a DC inverter to keep it in a saturated state. In this condition the inverter base input terminal is at -3 volts, the transistor base is at ground, and 1 ma current is drawn through the 3000 ohm base resistor.

Inverter load resistors, when clamped at -3 volts, have about 12 volts across their 1500 ohms, and they can accept about 8 milliamperes of current. Ideally, this would drive 8 units of BASE LOAD, but tolerance considerations limit the number to 7.

A "PULSE LOAD" is the load presented to a pulse source when driving the base of an inverter.

Pulse amplifiers are usually limited to driving 16 pulse bases. This number should be decreased if the bases are widely separated, and it can be increased to 18 if they are all close together. The series inductance and shunt capacity of the connecting wires can make the pulses at the end of a string of bases either large or small. Consequently, when a number near the maximum is being driven, the pulse amplitude should be carefully checked after installation. A terminating resistor in the 100-to-300 ohm range is desirable to reduce ringing on a heavily loaded pulse line.

A "PULSE LOAD" is also the load seen by a pulse source when driving one direct set or direct clear input of a flip-flop. The loading on a pulse source is approximately the same as when driving a base. One pulse source, of course, cannot drive both direct inputs of flipflops and inverter bases because the direct input pulses are positive from a normal ground level and base input pulses are negative from a normal ground level.

A "PULSED EMITTER LOAD" is the load seen by the collector of an inverter driving the pulse input to a flip-flop, pulse amplifier or delay. The pulse current goes through all the inverters in series with the pulse input, and it should be assumed to be the load on each of the series inverters.

A "DC EMITTER LOAD" is a load seen by the collector of an inverter driving a clamped load resistor. This load is also seen by the collector of an inverter which is driving an emitter in a network of inverters which is terminated by a clamped load resistor.



FIGURE 56

The collector of an inverter driving an emitter in a network of transistors must also supply the base current leaving the inverters higher in the chain. This number is normally small, but in complex networks it must be considered. An inverter can drive no more than one clamped load resistor and six bases of "on" inverters. Since transistors are almost symmetrical, this "on" base current can also flow through the collector of a transistor whose emitter is open, as shown in Figure 56. In this case, the collector of the bottom "on" transistor must carry the current A from the load resistor and the base currents from B, C and D.



DEC Power Supplies Provide Proper Voltages for Logical Operations



DEC HIGH CURRENT PULSE EQUIPMENT INCLUDES NEGATIVE AND POSITIVE CURRENT DRIVERS AND CURRENT CALIBRATORS

## MARGINAL CHECKING

Marginal checking is used in a system to find the margin of safety between the condition of a system and the point of failure. Marginal checking is normally used in routine maintenance to find deteriorating components before they cause system failure. In many instances routine marginal checking is not necessary due to the long life of modern transistors, but it is still invaluable in debugging a new system. Without marginal checking, a system may be assembled with a number of mistakes which do not cause failure but which do not provide the system with as much margin as it should have.

In systems made with DEC Modules, the +10 volt bias on inverters is varied for marginal checking. In most Modules, the +10 inputs are broken into two groups to make possible most critical marginal checking. In large systems, like the DEC Programmed Data Processor, the +10 lines to the Modules are broken down into several groups so that small portions of the system can be marginal checked at one time.

If the inverter transistor has marginal gain, it will fail when the +10 supply is increased less than 5 volts because the drive to the base of that transistor is lessened.

Reducing the positive bias on an inverter will detect noise on the inverter input or a condition where the input does not come sufficiently close to ground. Normal margins on a system are plus and minus 5 volts on the +10 volt supply.

# INDICATORS

In most systems an indicator lamp is connected to each flip-flop to show its logical state. In DEC Laboratory Modules the indicator lamps are built into the flip-flop units with their own transistor drivers.

Types 1669 and 1675 plug-in units are used to drive indicators with the System Modules. The indicator drivers are power transistors in an inverter circuit, very much like a logic inverter except that the 3000 ohm resistor in the base is not bypassed with a capacitor. In the high-speed lines, the 3000 ohm resistor is included in the flip-flop package and not in the 1675 package to avoid capacitive loading on the flip-flop output. However, in the low-speed line the base resistors are included in the 1669 package.

The load of the inverter is the incandescent lamp, which is tied to the -15 supply. When the inverter is on, the full 15 volts is across the lamp bulb. Normally, a GE 327 aircraft-type indicator

lamp bulb is used. This is a conveniently small bulb with very good life characteristics. It is rated at 24 volts, but when operated at 15 volts the light output is pleasant, and the life of the lamp is very long.

The DEC Type 1671 BCD Light Driver is designed to drive a decimal display from either a binary coded decimal register or a Gray coded decimal register. This unit decodes a decade (four flip-flops) into ten lines and amplifies the output. The output will produce up to 150 milliamperes at -20 volts. This is sufficient for a GE 47 lamp, such as those used in the Industrial Electronic Engineers Model 10000-47 decimal display unit.

# **BOOLEAN ALGEBRA**

NOTE: As mentioned in the Introduction, a knowledge of Boolean algebra is not a prerequisite to the performance of logic design with DEC Modules. However, Laboratory Modules and System Modules can be used to implement Boolean equations quickly and easily.

Boolean algebra was introduced in 1847 by an English mathematician, George Boole. The purpose of the algebra was to find a shorthand notation for the system of logic originally set forth by Aristotle. Aristotle's system dealt with statements which were considered to be either true or false, but never partially true or false. Boole's algebra was based on a single valued function with two discrete possible states.

Boolean algebra lay almost dormant until recent times. Today, however, it is gaining widespread recognition as an efficient method for handling any single valued function with only two possible states. When it is applied to binary arithmetic, the two states are ZERO and ONE. When discussing a switch, the two values are OPEN and CLOSED.



FIGURE B1

The convention used will be that the OPEN state corresponds to the ZERO state while the CLOSED state corresponds to the ONE state.

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FIGURE B2

If two switches, A and B, are connected in parallel to form a gate, inspection shows that the gate can only transmit information if A or B or both are in the transmitting state, i.e., CLOSED. This is written in equation form as

$$A + B = C$$

# (A or B equals C)

Figure B2 shows the parallel combination of two switches along with its equivalent inverter gate and a table giving the value of C for all possible values of A and B.



By adding a third gate in parallel, as in Figure B3, it becomes obvious how the OR function may be extended to any number of variables. This figure also serves to illustrate that the commutative and associative laws are valid for the OR function, i.e.,

$$A + B = B + A$$
  
 $(A + B) + C \equiv A + (B + C) \equiv A + B + C$   
50



FIGURE B4

If two or more gates are placed in series, the result is known as an AND gate. Inspection of the arrangement in Figure B4 shows that the resulting gate will transmit only if both A and B are CLOSED, i.e., equal to ONE. The equivalent equation in Boolean form is

$$AB = C$$
  
(A and B equal C)



FIGURE B5

Figure B5 demonstrates how the AND function is applied to more than one variable. The commutative and associative laws also hold.

$$AB = BA$$
$$A(BC) \equiv (AB)C \equiv ABC$$
$$51$$

# **IDENTITIES**



FIGURE B6

To enable the simplification of Boolean functions, there are many identities which are helpful. In Figure B6, the combinations of switches and corresponding equations demonstrate these identities.

#### COMPLEMENT

If two gates are connected so that the same signal will open both of them or close both of them simultaneously, then the switches are given the same symbol. If two gates are connected so that a single signal will open one gate while closing the other gate, and vice versa, then these gates are said to be the complement of each other. Thus, if one gate is labeled A, the other gate will be labeled  $\overline{A}$  (read "not A"). An entire function may also be complemented. For example,

if C = A(B + C)then  $\overline{C} = \overline{A(B + C)}$ 

The use of one label for more than one gate makes the following identities helpful:

$$A + A = A$$
  $A + \overline{A} = 1$   $\overline{A} = A$   
 $AA = A$   $A\overline{A} = 0$ 

# DE MORGAN'S LAWS

Two unique laws which can be applied only to Boolean algebra are known as De Morgan's laws.

$$\overline{\overline{A} + B} + \overline{C} + \dots + \overline{N} = \overline{\overline{A}}\overline{B}\overline{C} \dots \overline{N}$$
$$\overline{\overline{A}}\overline{B}\overline{C} \dots \overline{N} = \overline{\overline{A}} + \overline{\overline{B}} + \overline{\overline{C}} + \dots + \overline{\overline{N}}$$

These laws may be verified by constructing a table of various possible values.

## BOOLEAN ALGEBRA FOR USE WITH VOLTAGE LEVELS

Since DEC voltage levels have only two possible values, Boolean algebra can also be useful in the study of these levels.



FIGURE B7

The basic unit of DEC Logic is the transistor inverter. The simplest use of the inverter is to perform a complement. If the emitter is at ground and a signal is applied to the base, the resulting output is the complement of the base input.



FIGURE B8

A simple OR gate is formed by means of diodes, as shown in Figure B8. If A or B or C or D or E or F or any combination of these is negative, the resulting output is negative.

A similar unit with the diodes reversed will form an AND gate. Only if A and B and C and D and E and F are negative will the resulting output be negative.

Inspection of these diode units shows that the AND and OR gates will be interchanged if the levels are defined in the opposite manner. That is, if ground is defined as a ONE and negative is defined as a ZERO. This is a demonstration of De Morgan's law.



If the signals are manipulated without the encumbrance of a permanent sign convention, the same gate may perform many functions. Figure B9 shows an inverter which serves as an AND gate if the following definitions are used: A = 1 if negative, B = 1 if ground, C = 1 if ground. The same transistor can be used as an OR gate if the opposite definitions are made, i.e.: A = 1 if positive, B = 1 if negative, and C = 1 if negative.

For this reason, DEC uses the sign convention that the diamond arrowheads on signals indicate the required polarity for the desired action. A solid diamond denotes a -3 volt level for assertion, while a hollow diamond denotes a ground level for assertion. By using this method, it is possible to combine amplification and gating without added inversions as would otherwise be necessary. Several illustrations are shown in Figure B10.



FIGURE B10

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# DEC TECHNICAL BULLETINS

NOTE: DEC digital circuit packages are being renamed "Modules." As new bulletins are published, the two basic product lines will be referred to as "Laboratory Modules" instead of "Digital Test Equipment" and as "System Modules" rather than "System Building Blocks."

- DEC Building Blocks & Digital Systems (A-700B) short form catalog listing DEC's complete product line.
- DEC 10 Megacycle Building Blocks (A-710) describes new 5000 Series Digital Test Equipment and 6000 Series System Building Blocks.
- Expanded 100 Series DEC Digital Test Equipment (B-100) describes DEC's 5 megacycle patchcord units.
- New 3000 Series DEC Digital Test Equipment (B-3000) describes DEC's 500 kilocycle patchcord units.
- Expanded 1000 Series DEC System Building Blocks (C-1000A) describes DEC's 5 megacycle plug-in units.
- New 4000 Series DEC System Building Blocks (C-4000A)—describes DEC's 500 kilocycle plug-in units.
- DEC Basic Logic Kit (E-150) describes a basic selection of DEC Digital Test Equipment and Accessories which can be used to perform a variety of logical operations.
- DEC Programmed Data Processor (F-10) describes DEC's PDP-1 high-speed, solid state, general purpose computer.
- DEC Memory Tester Type 1512 (F-1512A) describes DEC's 1500 Series testers for coincident current core memories.
- DEC Memory Tester Type 1514 (F-1514) describes DEC's 1500 Series testers for word address and coincident current core memories.
- DEC Automatic Memory Core Tester Type 2101 (F-2101)—describes DEC's automatic tester for ferrite magnetic memory cores.
- DEC Programmable Pulse Generator Type 2104 (F-2104)—describes DEC's versatile new pulse generator system.
- DEC Memory Exerciser Type 2201 (F-2201) describes DEC's exercisers for coincident current core memory systems.

Copies of the above bulletins are available on request from the DEC Sales Department, 146 Main Street, Maynard, Massachusetts, or 8820 Sepulveda Boulevard, Los Angeles 45, California.

# **INFORMATION REQUEST**

Please arrange for me to receive future editions of the "Digital Logic Handbook" at no obligation. I would also like to have the following technical bulletins: As new Modules are added to the Digital line and as new applications are developed, this information will be incorporated in revised and expanded editions of the "Digital Logic Handbook."

If you would like to receive future editions at no obligation, just complete and return this reply card. And if you would like additional information on any DEC products, please note this in the space provided.

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